



Extreme Mass Loss in Low-mass Type Ib/c Supernova Progenitors

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Abstract

Many core-collapse supernovae (SNe) with hydrogen-poor and low-mass ejecta, such as ultra-stripped SNe and type Ibn SNe, are observed to interact with dense circumstellar material (CSM). These events likely arise from the core collapse of helium stars that have been heavily stripped by a binary companion and have ejected significant mass during the last weeks to years of their lives. In helium star models run to days before core collapse we identify a range of helium core masses $\approx 2.5\text{--}3 M_{\odot}$ whose envelopes expand substantially due to the helium shell burning while the core undergoes neon and oxygen burning. When modeled in binary systems, the rapid expansion of these helium stars induces extremely high rates of late-stage mass transfer ($\dot{M} \gtrsim 10^{-2} M_{\odot} \text{ yr}^{-1}$) beginning weeks to decades before core collapse. We consider two scenarios for producing CSM in these systems: either mass transfer remains stable and mass loss is driven from the system in the vicinity of the accreting companion, or mass transfer becomes unstable and causes a common envelope event (CEE) through which the helium envelope is unbound. The ensuing CSM properties are consistent with the CSM masses ($\sim 10^{-2}\text{--}1 M_{\odot}$) and radii ($\sim 10^{13}\text{--}10^{16}$ cm) inferred for ultra-stripped SNe and several type Ibn SNe. Furthermore, systems that undergo a CEE could produce short-period neutron star binaries that merge in less than 100 Myr.

Unified Astronomy Thesaurus concepts: Core-collapse supernovae (304); Binary stars (154); Stellar mass loss (1613); Circumstellar matter (241); Stellar evolution (1599)

1. Introduction

Many types of core-collapse supernovae (SNe) show signs of interaction with dense circumstellar material (CSM), likely created by extreme mass loss at the end of the supernova (SN) progenitor's life (Hosseinzadeh et al. 2019; Pastorello et al. 2008, 2015a, 2015b; Gal-Yam et al. 2014). Type Ibn SNe are characterized by interaction with hydrogen-poor and helium-rich CSM, which produces spectra dominated by narrow helium (He) lines and powers early-time light curves that often rise and decay quickly. Typical rise times of $\lesssim 15$ days and peak magnitudes of $M_R \sim -19$ to -20 mag in these events indicate ejecta masses $M_{\text{ej}} = 1\text{--}5 M_{\odot}$ and ^{56}Ni masses $M_{\text{Ni}} \lesssim 0.1 M_{\odot}$ (Ho et al. 2021; Gangopadhyay et al. 2022; Maeda & Moriya 2022). These SNe are thought to originate from massive stars that have previously lost their hydrogen envelopes, then expelled helium-rich CSM just before core collapse.

A few events have been discovered with even lower M_{ej} and M_{Ni} , classified as ultra-stripped SNe (USSNe). For example, the short decline time of type Ic SN iPTF 14gqr indicates a small ejecta mass of $M_{\text{ej}} \sim 0.2 M_{\odot}$ (De et al. 2018), and consequently a low precollapse mass of $M_{\text{He}} \sim 1.6 M_{\odot}$ (assuming a baryonic NS mass of $M_{\text{NS}} = 1.4 M_{\odot}$). The type Ib SN 2019dge has $M_{\text{ej}} = 0.4 M_{\odot}$, implying a precollapse mass $M_{\text{He}} \sim 1.8 M_{\odot}$ (Yao et al. 2020). Bright rapidly rising early-time light curves and flash-ionized He emission in early spectra indicate extended CSM in SN iPTF 14gqr and SN 2019dge. Another type of interacting SNe, type Icn SNe, exhibit narrow emission lines from the recombination of ionized carbon and oxygen instead of He. With comparable peak luminosities to type Ibn

SNe but low M_{Ni} and M_{ej} , type Icn SNe have been proposed to arise from similar channels to USSNe (Pellegrino et al. 2022a).

Highly stripped helium stars are the probable progenitors of USSNe. Stars that have lost their hydrogen envelopes after hydrogen burning through case B mass transfer (MT) form stripped stars from their He cores. Stripped stars with $M_{\text{He}} \lesssim 4 M_{\odot}$ expand again and initiate so-called case BB MT in systems with final separations of less than a few $100 R_{\odot}$ after case B MT (Habets 1986a, 1986b), thereby losing a significant amount of their He envelope as well. At core collapse, their low precollapse masses can explain the requisite M_{ej} of USSNe (Tauris et al. 2013, 2015). When the USSNe is formed from the initially less-massive star in the binary, such systems are likely the most common progenitors of compact NS binaries (Dewi & Pols 2003; Tauris et al. 2013, 2015).

Previous work (Yoon et al. 2010; Tauris et al. 2013, 2015; Zapartas et al. 2017; Laplace et al. 2020) has modeled case BB MT in detail to make predictions for mass loss and the final fate of the progenitor. Thus far, most stellar models do not predict large amounts of CSM near the progenitor system as detected in several USSNe and type Ibn SNe. Yet the vast majority of stripped progenitor models omit the evolution onward from oxygen/neon (O/Ne) burning, and they miss crucial physics that transpires during these final years of the star's lifetime that may explain such SN observations (though see Jiang et al. 2021 for an exception). We find that helium stars of masses $\approx 2.5\text{--}3 M_{\odot}$ rapidly reexpand while the core burns O/Ne, which initiates high rates of late-stage MT weeks to decades before core collapse that may produce CSM.

2. Methods

We use MESA (version r15140, Paxton et al. 2011, 2013, 2015, 2018, 2019) to model 1D stellar evolution up to silicon (Si) burning of single stripped stars at $Z = 0.02$ with

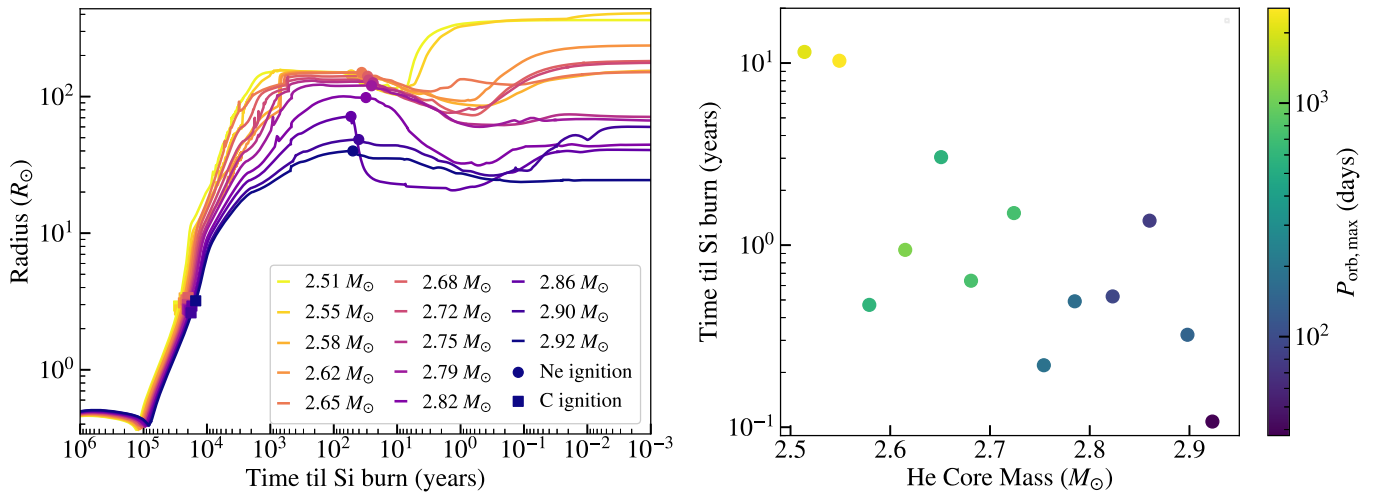


Figure 1. Left: evolution of the radius of single stripped stars as a function of time until Si burning. The legend labels the initial He core mass of each stripped star. Each star expands after He burning and throughout C burning, then contracts and reexpands during O/Ne burning. Right: time before Si burning of the stripped stars’ second expansion. Points are colored by the maximum orbital period at which the star will fill its Roche lobe in a binary with a $1.4 M_{\odot}$ companion star.

$2.5 M_{\odot} \lesssim M_{\text{He}} \lesssim 3 M_{\odot}$.³ The timing of removing surface hydrogen, the amount of hydrogen remaining, and the inclusion of stellar winds each affect how initial mass M_{ZAMS} maps to He core mass M_{He} after core He burning. In this work, we remove the entire hydrogen envelope of stars with initial masses $M_{\text{ZAMS}} = 13.8\text{--}15 M_{\odot}$ once core hydrogen burning ends and we evolve without wind mass loss. Ultimately, the relation between initial and helium star mass is not central to the result, and we find that the behavior of our models depends primarily on the He core mass after core He burning. Throughout, we label our models by these initial He core masses M_{He} .

We also model the stripped stars in binaries at a range of orbital periods from 1 to 100 days to estimate the ensuing MT rates. For our binary models, we consider the fiducial scenario where the stripped star formed from the initially less-massive star in the binary, so its companion is an $M_c = 1.4 M_{\odot}$ neutron star (NS), represented by a point mass. We use a modified version of the implicit MT scheme of Kolb & Ritter (1990) for Roche lobe overflow. Since this prescription assumes an ideal gas equation of state, it underestimates mass-loss rates for surface layers dominated by radiation pressure; to address this, we revise the scheme to compute the pressure from the stellar model (e.g., Marchant et al. 2021). We assume nonconservative MT, where the mass is removed from the system in the vicinity of the accretor as a fast wind. As we find that MT rates during both case BB and late-stage mass loss are many orders of magnitude larger than the Eddington accretion limit of an NS ($\dot{M}_{\text{edd}} \sim 4 \times 10^{-8} M_{\odot} \text{ yr}^{-1}$), we expect that nearly 100% of the mass is lost from the system (as in, e.g., Tauris et al. 2015), though mass loss out of the L2 and/or L3 points could modify the binary’s angular momentum loss (see Section 4).

3. Results

3.1. Single Star Evolution

Stripped stars with initial masses $2.5 M_{\odot} \lesssim M_{\text{He}} \lesssim 3 M_{\odot}$ expand during several phases of their evolution. In the left panel of Figure 1, the radii of the stripped stars increase by 2 orders of magnitude during C burning beginning $\sim 10^5$ yr

before Si burning, which in a binary system causes case BB MT. Notably, the stars contract after C-shell burning (a few decades before Si burning) and expand by a factor of a few again during O/Ne burning, which can initiate late-stage MT.

The right panel of Figure 1 plots the time before Si burning when this late expansion occurs versus stripped star mass M_{He} . For higher masses, expansion occurs months before Si burning during late O burning, but lower masses expand again a decade before Si burning. However, the expansion is driven not by core burning but rather by intense He burning at the base of the helium envelope. This behavior can be understood by the mirror principle (e.g., Kippenhahn et al. 2012; Laplace et al. 2020), in which core contraction after certain burning phases (e.g., C-shell burning) causes the temperature of the He burning shell to increase. As the temperature-sensitive triple-alpha energy generation rate increases significantly, the envelope of the star expands in response to the intensified heating at its base.

From the maximum radius to which each stripped star expands, we estimate the maximum orbital period P_{orb} for the star to fill its Roche lobe during late-stage MT. For a companion mass of M_c , the mass ratio is $q = M_c/M_{\text{He}}$. Then the ratio of the Roche lobe radius R_{RL} to semimajor axis a is approximately (Eggleton 1983)

$$\frac{R_{\text{RL}}}{a} = 0.49 \frac{q^{2/3}}{0.6q^{2/3} + \log(1 + q^{1/3})}. \quad (1)$$

Setting each star’s maximum radius during O/Ne burning to R_{RL} and applying Kepler’s third law gives the maximum orbital period for Roche lobe overflow, $P_{\text{orb,max}}$. In the right panel of Figure 1, points are shaded by the value of $P_{\text{orb,max}}$, which tends to decrease with He mass. The stripped stars may initiate late-stage MT up to orbital periods of months to years.

3.2. Binary Evolution

Figure 2 shows the MT rates \dot{M} and accumulated mass loss of our binary models at $P_{\text{orb}} = 100$ days, 10 days, and 1 day. Once the models achieve very high mass-loss rates $\dot{M} \gtrsim 10^{-3} M_{\odot} \text{ yr}^{-1}$, MESA systematically encounters numerical difficulties at the surface of the star, where mass layers are rapidly stripped. In

³ The data are available on Zenodo under an open-source Creative Commons Attribution license: [10.5281/zenodo.7106182](https://zenodo.org/record/7106182).

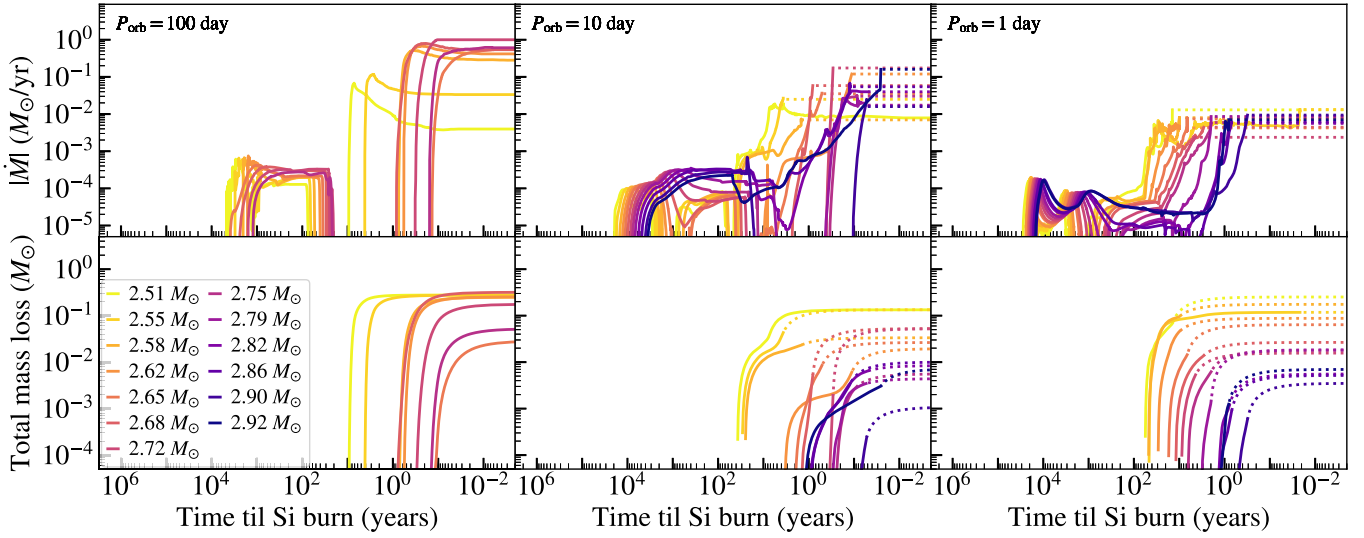


Figure 2. The mass-loss rates and accumulated mass loss of the helium star models, each of which is placed in a binary with a $1.4 M_{\odot}$ compact companion at the initial orbital periods listed in the top panels. The legend indicates the initial mass of each helium star. For simulations that end before Si burning, we assume that \dot{M} remains steady until Si burning and extrapolate the accumulated mass loss until Si burning, shown as dotted lines.

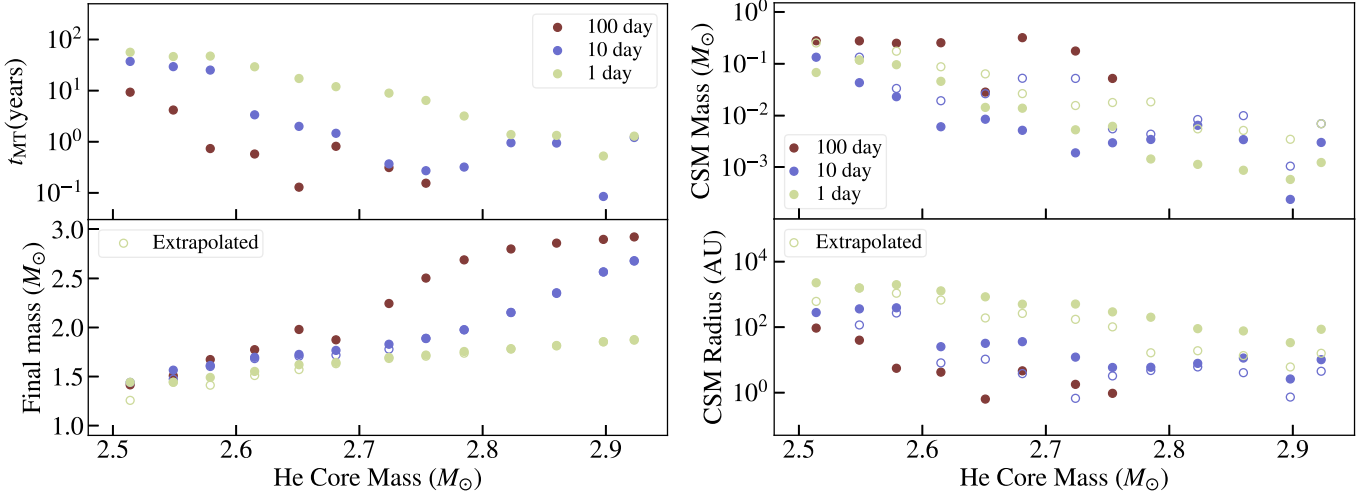


Figure 3. Properties of each binary system undergoing late-stage mass loss. Points are plotted as a function of the helium star’s initial mass, and colors correspond to the initial orbital period given in the legend. Dots represent mass loss up to the end of the solid lines in Figure 2, and open circles include the extrapolated mass loss shown as dotted lines in Figure 2. Top left: time before Si burning when late-stage MT ensues, t_{MT} , as defined in Section 3.2. Bottom left: final mass of each stripped star after case BB and late-stage MT. Right: predicted mass (top) and radius (bottom) of CSM due to late-stage mass loss.

models where MESA is unable to evolve the MT up to Si burning, we estimate the time until Si burning by comparison with single-star models and also extrapolate further potential mass loss by assuming that \dot{M} plateaus until Si burning. This approximates the behavior of models that do evolve to Si burning (e.g., $P_{\text{orb}} = 100$ days); in practice, the extrapolation may be a lower limit to the true mass loss since MT rates are usually increasing sharply when models terminate. Binary models at larger P_{orb} begin late-stage MT later in the donor’s lifetime, and the highest-mass models $M_{\text{He}} \gtrsim 2.8 M_{\odot}$ do not expand enough to fill their Roche lobes at $P_{\text{orb}} = 100$ days. At $P_{\text{orb}} = 1$ day, models do not fully detach from their Roche lobes after C burning, but late-stage MT clearly manifests as \dot{M} increases by $\sim 2\text{--}3$ orders of magnitude during O/Ne burning.

Typical mass-loss rates are $10^{-3}\text{--}10^{-1} M_{\odot} \text{ yr}^{-1}$ during late-stage MT. Though our binary models at $P_{\text{orb}} = 100$ days rise to $\dot{M} \sim 0.1\text{--}1 M_{\odot} \text{ yr}^{-1}$ in the last weeks to months before Si burning, these highly uncertain values occur because the

models greatly overfill their Roche lobes during these phases, causing the MT scheme in MESA to break down. We define the time until Si burning when late-stage MT occurs, t_{MT} , when $\dot{M} > 5 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$, significantly exceeding the case BB MT rate of $\sim 10^{-4} M_{\odot} \text{ yr}^{-1}$. In the top left panel of Figure 3, t_{MT} is shown for each He star. The mass-loss rate tends to rise months to years before Si burning for models of larger mass and longer P_{orb} , but late-stage MT can occur years to decades before Si burning for lower mass and shorter P_{orb} .

The bottom left panel of Figure 3 shows the final masses after both case BB and late-stage mass loss, which range between ~ 1.4 and $2.9 M_{\odot}$. The low precollapse masses imply small SN ejecta masses $\lesssim 1.5 M_{\odot}$, assuming $M_{\text{NS}} = 1.4 M_{\odot}$. Compared to similar models in Tauris et al. (2015), our MT rates during C burning and final masses are consistent with their results. Following their argument that models with final CO core masses $\gtrsim 1.43 M_{\odot}$ will reach iron core collapse, we expect that our lowest-mass models $2.5\text{--}2.55 M_{\odot}$ may become

electron-capture SNe, while the majority of our models $\gtrsim 2.6 M_{\odot}$ will undergo core collapse. The final fate of our models corresponds to slightly different initial He core masses than in Tauris et al. (2015), as our stellar evolution implementation produces slightly higher CO core masses for the same initial mass.

3.3. CSM Properties

To estimate the properties of CSM ensuing from late-stage MT, we treat each donor’s mass loss as ejected from the system in the vicinity of the accretor. Stable MT at these high rates may form an advection-dominated geometrically thick accretion disk around the companion that can drive a large proportion of mass from the outer disk, lost through the L2 point (Pejcha et al. 2016; Lu et al. 2022). Motivated by this scenario, we assume that lost mass leaves with the orbital velocity at the L2 point. In reality, the ejection speed may vary due to initial conditions and torquing by the binary, and ejection velocities and CSM radii smaller by a factor of ~ 3 may be more realistic (Hubová and Pejcha 2019).

Shells of expelled material form at a distribution of radii around the system, so we perform a mass-weighted average of these radii to calculate the characteristic CSM radius. The integrated mass-loss rate at core collapse equals the total CSM mass in each system. As shown in the right panel of Figure 3, we predict CSM masses ranging from $10^{-3} M_{\odot}$ for $\sim 2.9 M_{\odot}$ progenitors up to $\sim 3 \times 10^{-1} M_{\odot}$ for ~ 2.5 – $2.7 M_{\odot}$ progenitors. As it originates from stripping of the He envelope, the CSM produced by our models is He-rich, with He mass fractions $\gtrsim 0.7$ for the majority of the CSM mass.

In our models, the orbital velocity at L2 increases from $\sim 100 \text{ km s}^{-1}$ at $P_{\text{orb}} \approx 100$ days to $\sim 500 \text{ km s}^{-1}$ at $P_{\text{orb}} \approx 1$ day. Mass ejected from the system at these velocities reaches radii of ~ 1 – 10^4 au. Lower mass and shorter P_{orb} models tend to produce CSM at larger radii, as late-stage MT begins earlier in the evolution and in the latter case is ejected with larger velocities.

3.4. Common Envelope Events

The sharply rising MT rates in all our models may indicate the onset of unstable MT, leading to a common envelope event (CEE). In this case, we would expect the companion to inspiral into the envelope of the ultra-stripped star, with total mass M_s at the onset of CEE. We predict the outcome by assuming that unstable MT ensues soon after \dot{M} exceeds $5 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$, and that the inspiral will terminate once the change in the orbital energy is sufficient to unbind the entire envelope of mass $M_{s,\text{env}}$ exterior to the C/O core of mass $M_{s,\text{core}}$. To quantify this, we use the α energy formalism:

$$E_{\text{bind}} = \alpha \Delta E_{\text{orb}} \quad (2)$$

$$= \alpha \left(-\frac{GM_s M_c}{2a_i} + \frac{GM_{s,\text{core}} M_c}{2a_f} \right), \quad (3)$$

where $E_{\text{bind}} = \int_{\text{core}}^{\text{surface}} -\frac{Gm}{r} + \epsilon(m) dm$, where ϵ is the specific internal energy. Here, the CE efficiency α parameterizes the fraction of orbital energy used to eject the envelope; M_c is the companion mass, and a_i is the initial orbital separation, determined by Equation (1) with R_{RL} equal to the stellar radius at the CE onset. We solve for the final orbital separation a_f , which satisfies this equation for each binary model assuming

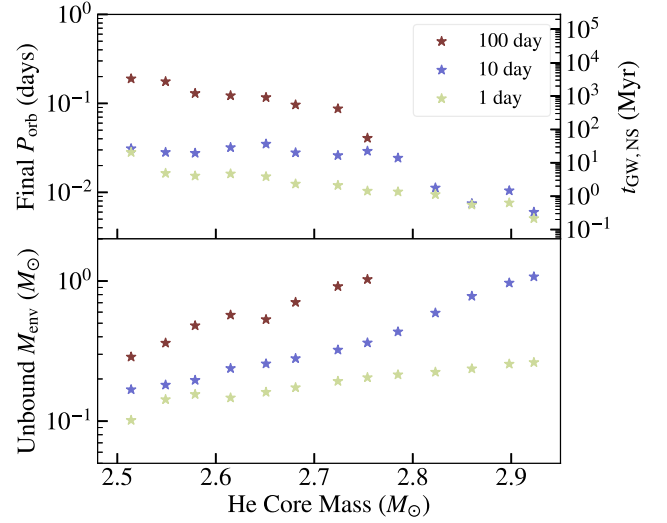


Figure 4. Properties of the binary systems after a CEE, assuming unstable MT begins once $\dot{M} > 5 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$ and that the inspiral ends once the NS unbinds the envelope down to the CO core. Points are plotted as in Figure 3 as a function of each stripped star’s initial He core mass. Top: values on the left axis show the final orbital period of each system after the CEE. The right axis values are the gravitational-wave merger timescales for a binary system consisting of two neutron stars orbiting at the periods of the left axis. Bottom: envelope mass unbound by the CEE.

$\alpha = 0.3$, consistent with observational constraints (Zorotovic et al. 2010; Zorotovic & Schreiber 2022). Though defining the final mass after the CEE is uncertain, we find that our results are not sensitive to this choice; here, we set the final mass to be the CO core mass at the onset of the CEE.

Figure 4 shows final orbital periods of our models after the CEE. In the vast majority of systems, the binary exits the CEE at orbital periods $\lesssim 4$ hr, which can merge within Hubble time. This orbital separation is too small to admit a main-sequence (MS) star, so unstable MT with an MS companion will likely result in a stellar merger followed by an unusual supernova. White dwarf or neutron star companions, however, can likely eject the envelope before merging with the CO core. The gravitational-wave orbital decay timescale for a binary of two neutron stars $M_{\text{NS}} = 1.4 M_{\odot}$ at each orbital period, $t_{\text{GW,NS}}$, is shown for comparison on the right axis. Models with larger M_{He} and shorter initial P_{orb} can reach final P_{orb} of under 30 minutes, corresponding to $t_{\text{GW,NS}} \lesssim 10$ Myr.

The bottom panel of Figure 4 shows the mass of the unbound envelope due to the CEE, which increases with M_{He} from $\sim 10^{-1}$ to $1 M_{\odot}$ for more massive progenitors. These CSM masses typically exceed our estimates for the stable MT scenario by a factor of ~ 10 , though we reiterate that those values are likely to be lower limits in many cases. We estimate the CSM radii produced by a CEE by assuming the envelope is ejected with a terminal velocity equal to the star’s pre-CEE surface escape velocity (consistent with $\alpha \sim 1/3$).

3.5. Comparisons to USSNe and Type Ibn/Icn SNe

Figure 5 compares CSM masses and radii inferred for several interacting SNe with our model predictions. We include our estimates for stable late-stage mass loss (Section 3.3) and from mass ejected due to a CEE (Section 3.4). In general, methods of observationally constraining the mass and radius of CSM are likely uncertain by a factor of a few (Chatzopoulos et al. 2012, 2013;

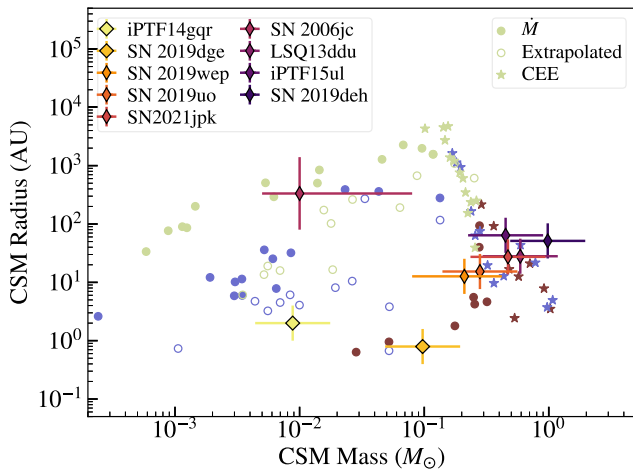


Figure 5. Dots and open circles are predicted mass vs. radius of CSM due to late-stage mass loss (Figure 3, Section 3.3). Star symbols are predicted mass and radius of material unbound during the CEE (Figure 4, Section 3.4). Colors indicate initial P_{orb} as in Figure 3. Points with error bars are estimated CSM properties of USSNe (square diamonds) and type Ibn SNe (thin diamonds). All are given error bars of at least a factor of 2 in each direction to account for systematic uncertainties in the modeling.

De et al. 2018), so we show inferred values with error bars of at least a factor of 2 in each direction.

In the vast majority of our models, the predicted CSM is H poor and He rich, so interaction with the CSM during an SN would likely produce spectra classified as type Ibn. Several type Ibn SNe are shown in Figure 5 as thin diamonds. SN 2006jc (Anupama et al. 2009) may be matched by a range of $P_{\text{orb}} = 1$ and 10 day models for late-stage MT, whereas CSM estimates for iPTF 15ul, SN 2019wep, and SN 2019uo (Pellegrino et al. 2022b) fall within the late-stage MT estimates for initial $P_{\text{orb}} = 100$ days. All type Ibn events shown, including SN 2019deh, SN 2021jpk, and LSQ 13ddu (Clark et al. 2020; Pellegrino et al. 2022b), can be explained by CSM produced in a CEE in several $P_{\text{orb}} = 1, 10,$ and 100 day models.

Estimates from modeling shock-cooling emission of extended material around the progenitors in USSNe iPTF 14gqr and SN 2019dgc, shown as the blue and orange diamonds, are consistent only with our smallest CSM radii predictions. Our models for late-stage MT with initial $P_{\text{orb}} = 10$ days and $M_{\text{He}} = 2.6\text{--}2.9 M_{\odot}$ can explain the envelope mass $M_e \approx 0.01 M_{\odot}$ and radius $R_e \gtrsim 2$ au derived for iPTF 14gqr (De et al. 2018). Similar-mass late-stage MT models with initial $P_{\text{orb}} = 100$ days can explain observed material at ~ 1 au for SN 2019dgc (Yao et al. 2020).

In addition, outer CSM regions located beyond a few to tens of astronomical units have been detected in iPTF 14gqr and SN 2019dgc. Estimates from He II line emission of the mass of helium in this outer CSM provide lower limits of $\gtrsim 3 \times 10^{-5} M_{\odot}$ for SN 2019dgc and $\gtrsim 10^{-2} M_{\odot}$ for iPTF 14gqr. CSM produced from late-stage MT fits well with the properties of outer regions of CSM in both USSNe. In addition, our models routinely attain the inferred presupernova mass-loss rates of $\gtrsim 10^{-2} M_{\odot} \text{ yr}^{-1}$ and $\gtrsim 10^{-4} M_{\odot} \text{ yr}^{-1}$, respectively, for iPTF 14gqr and SN 2019dgc.

Interaction with CSM has been detected in several type Icn SNe (Gal-Yam et al. 2022; Pellegrino et al. 2022a). These events mainly show narrow C/O emission lines, though none are conclusively devoid of He, and the type Icn SN 2019jc in particular has an He II feature. With the exception of the values

derived for SN 2019hgp by Gal-Yam et al. (2022); the type Icn SNe tend to produce more massive CSM than our models predict. Most importantly, these events likely require lower He mass fractions than ejected by our models (Dessart et al. 2022), which typically have $X_{\text{He}} \sim 0.8$ and $X_{\text{CO}} \sim 0.2$.

4. Discussion and Conclusions

The fiducial scenario addressed by our binary models describes an He star, formed from the initially less-massive star (the secondary) in a binary, with an NS companion evolved from the initially more massive star (the primary). However, primary stars within our modeled mass range will exhibit the same behavior. If the primary has a low-mass MS companion, case B MT is expected to be dynamically unstable leading to a CEE. The low-mass MS star could survive the inspiral and exit CEE in a close orbit with the He star—these are likely the progenitors of low-mass X-ray binaries (e.g., Verbunt 1993; Kalogera & Webbink 1998). If the companion is massive, case B MT is likely stable and may widen the orbit, but for post-MT separations less than a few $100 R_{\odot}$ the He star can still overflow its Roche lobe during late-stage expansion. Thus, the late-stage MT displayed by our stripped star models may affect the appearance of a type Ib/c SN coming from either primary or secondary stars with $M_{\text{He}} \sim 2.5\text{--}3 M_{\odot}$. We note that wave heating driven by core convection can also lead to envelope expansion that may similarly initiate binary interaction (McIey & Soker 2014; Wu & Fuller 2022).

At the extreme MT rates predicted, the dynamics of the ejected mass are uncertain. Since the donor may greatly overflow its Roche lobe, mass may also flow out of the donor’s outer Lagrange point (L3 if the donor is more massive; Linial & Sari 2017; Marchant et al. 2021). Even if the companion is not a compact object, the high MT rates, if stable, may form a geometrically thick accretion disk around the companion. The disk will be super-Eddington even at large radii, such that L2 mass loss is predicted (Lu et al. 2022). The ensuing circumbinary outflow may cause appreciable additional angular momentum loss given the larger lever arm of the L2 point. This effect may shrink the orbital separation more rapidly, increasing and potentially destabilizing the MT rates. In preliminary tests, we have noticed a $\sim 20\%$ increase in the MT rate if we change the specific angular momentum of the mass lost to that of the L2 point.

However, the ejection velocities of $\sim 200 \text{ km s}^{-1}$ predicted in this framework tend to be lower than estimated from line widths in observed SNe. In the case of accretion onto a compact object, the disk around the accretor may launch a super-Eddington wind that sweeps up the slower outflow from the L2 point. It is also unclear how the ejected mass will be distributed. Though we report only a single CSM radius, the material will certainly cover a large radial extent and may not have a smooth or spherically symmetric profile.

If the MT becomes dynamically unstable, the accretion disk scenario is superseded by a CEE, as explored in Section 3.4. Our models with $P_{\text{orb}} = 100$ days appear highly susceptible to a CEE, as they reach very high MT rates $\dot{M} \sim 1 M_{\odot} \text{ yr}^{-1}$, which approach the dynamical regime of MT. They also have fully convective envelopes at the onset of late-stage MT and therefore are more inclined to lose MT stability. Once P_{orb} decreases to 1 day, models instead host only a very thin surface convective region. Hence, late-stage MT in binaries at long P_{orb} may result in CEEs that eject $\sim 1 M_{\odot}$, while binaries at shorter

P_{orb} may remain stable due to their mostly radiative envelopes. The former may account for many of the observed type Ibn SNe, while the latter may account for USSNe with He-rich CSM. Both scenarios may contribute to NS mergers, depending on the degree of orbital decay during the CEE or late-stage MT.

We roughly estimate the birth rate of progenitor systems that exhibit late-stage MT in order to compare with the rate of type Ib/c SNe that they may produce. The volumetric rate of type Ib/c SNe is $\sim 2.5 \times 10^{-5} \text{ Mpc}^{-3} \text{ yr}^{-1}$ (Li et al. 2011; Frohmaier et al. 2021). Given that type Ib/c SNe are thought to arise from binaries with a stripped star component, the type Ib/c rate approximates the birth rate of such systems, regardless of whether the primary or secondary star produces the SN. Our He star models could produce late-stage MT as either the primary or secondary star, and they represent the low-mass subset of type Ib/c SN progenitors. Binaries producing late-stage MT include at least one star with $M_{\text{ZAMS}} \sim 13\text{--}15 M_{\odot}$, whereas we assume systems contributing to the ordinary type Ib/c rate contain at least one star with $M_{\text{ZAMS}} \gtrsim 15 M_{\odot}$. By integrating the IMF (Kroupa 2001), we find that systems with late-stage MT constitute $\sim 11\%$ of type Ib/c SN progenitors. Thus, we estimate a birth rate for systems that exhibit late-stage MT of $\sim 3 \times 10^{-6} \text{ Mpc}^{-3} \text{ yr}^{-1}$. To compare to the rates of type Ibn SNe, we note that the Zwicky Transient Facility catalog estimates ~ 10 type Ibn SNe per ~ 900 CCSNe (Perley et al. 2020). Maeda & Moriya (2022) estimate $\sim 1\%$ of CCSNe are type Ibn SNe, giving a volumetric rate of $\sim 10^{-6} \text{ Mpc}^{-3}$, though these rates may be underestimates since such brief transients can be missed by surveys. Moreover, the calculation above likely overestimates the birth rate, as some massive star binaries may evolve to wide separations where late-stage MT does not occur, and some type Ib/c SNe may originate from merging systems. Thus, the birth rate of our progenitor systems appears to be roughly compatible with the type Ibn SN rate. Our model progenitors are also consistent with expectations from Hosseinzadeh et al. (2019), which found that Type Ibn SNe originated from relatively low-mass stars.

At the high MT rates seen in all our models, there is a very high degree of Roche lobe overflow that the MESA MT schemes do not capture well. More detailed modeling will be necessary to quantify more accurate late-stage MT rates. Nevertheless, the values presented here are conservative estimates for models where we see the MT rates increasing toward the end of our simulations. Additional sources of angular momentum loss not modeled here will serve only to exacerbate Roche lobe overflow through faster orbital decay. Ultimately, late-stage MT initiated during O/Ne burning will unavoidably lead to extremely high MT rates that can considerably influence the properties of these binary systems in the final years before core collapse.

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